

MAGIC SQUARES

$n \times n$ square, filled with
 $1, 2, 3, \dots, n^2$
such that all rows, columns, and
diagonals have the same sum

3x3			sums
2	7	6	15
?			15
			15
15	15	15	15

PROCEDURE:

States are configurations of $1, \dots, 9$ in a 3×3 square.

Transition from one state to another by:

- swap two numbers
- swap two rows or columns

Frequency function: big for a magic square
small for a square that is far from magic

$$f(\text{square}) = \max | \text{sums} - 15 |$$

$$\text{frequency distribution: } e^{-f(\text{square})/\sigma^2}$$

Simulate, decreasing σ^2 slowly,

If we are lucky, the simulation will produce a magic square.

IMPLEMENTATION:

How do we store a square in memory?

How do we compute row/col/diag sums?

How do we propose a random transition?

SWAPPING: How do we swap the values in two variables a and b?

~~a = b~~
~~b = a~~

```
temp = a
a = b
b = temp
```

In Python:

```
a, b = b, a
```

Replace a and b by matrix entries/rows/cols.

```
temp = np.copy(a)
a = b
b = temp
```