

isPrime[n]: returns True if n is prime,  
and False otherwise

Trial Division: see if n is divisible by  
any number 2, 3, 4, 5, ...,  $\lfloor \sqrt{n} \rfloor$

greatest integer less than  
or equal to  $\sqrt{n}$

### Implementation 1:

"Flag" — starts False, but will be  
set True if we find a divisor

loop over  
k from  
2 to  $\sqrt{n}$

```
isPrime[n_] := Module[{foundDivisor = False},
  Do[
    If[Divisible[n, k], foundDivisor = True],
    {k, 2, Sqrt[n]}
  ];
```

← if k divides n, then  
set foundDivisor to True.

```
!foundDivisor (* return value *)
];
```

NOT →

If no divisor is found, then  
n is prime.

If a divisor is found, then  
n is not prime.

### Implementation 2:

divisor to test

OR: ||

```
isPrime2[n_] := Module[{foundDivisor = False, d = 2, m = Sqrt[n]},
```

AND

max possible divisor

loop until  
a divisor  
is found  
or  $d > \sqrt{n}$

```
While[!foundDivisor && d ≤ m, ← conditions
  If[Divisible[n, d], foundDivisor = True];
  d++; increment d
];
```

```
!foundDivisor (* return value *)
]
```

**Print:** prints some value to the screen.

**Return:** sends a value back to wherever the module was called. It may or may not be printed on screen.

### Implementation 3:

```
isPrime3[n_Integer] := Module[{m = Sqrt[n]},  
  Catch[  
    Do[  
      If[Divisible[n, d], Throw[False]],  
      {d, 2, m}  
    ];  
    True  
  ] (* the Module returns the "caught" value *)  
]
```

If  $d$  divides  $n$ , then "throw" the value `False`. This interrupts the loop and transfers control to the enclosing `Catch` block.

The `Catch` statement has the value `False`.

If no divisor is found, then the `Catch` block has the value `True`.

The value of the `Catch` block is the module's return value.

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## LISTING PRIMES

`listPrimes[n]`: return a list of all primes up to  $n$ .

Plan: primes = { }

loop:  $k$  goes from 2 to  $n$

if  $k$  is prime, put it in the list primes

return primes list

# SIEVE OF ERATOSTHENES

2, 3, ~~4~~, 5, ~~6~~, 7, ~~8~~, ~~9~~, ~~10~~, 11, ~~12~~, 13, ~~14~~, ~~15~~,  
~~16~~, 17, ~~18~~, 19, ~~20~~, ~~21~~, ~~22~~, 23, ~~24~~, ~~25~~, ~~26~~, ~~27~~, ~~28~~, ...

How can we implement the sieve in Mathematica?

Make a plan on paper, then code in Mathematica.