

# RSA Encryption (of numbers)

1. Choose 2 prime numbers  $p, q$  (30 digits each).  
*secret*
2. Multiply:  $n = pq$   
*public*
3. Compute the totient:  $\lambda(n) = \text{LCM}(p-1, q-1)$   
*secret*      *least common multiple*
4. Choose an encryption key:  $e$  (4 or more digits is good)  
*public*      **NEED:  $\text{GCD}(e, \lambda) = 1$**
5. Compute your decryption key:  $d = \text{mod. inverse of } e \pmod{n}$   
*secret*       $\hookrightarrow de \equiv 1 \pmod{n}$

**ENCRYPT:** Let  $m$  be a "message" (that is, a number between 0 and  $n$ )

Compute:  $C = m^e \pmod{n}$

*"cypher" encrypted message*

*( $e, n$ ) is the public key of the intended recipient*

Post  $C$  for your recipient to see.

**DECRYPT:** compute  $C^d \equiv (m^e)^d \equiv m^{ed} \equiv m^1 = m \pmod{n}$   
*private key of the recipient*

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## TEXT TO NUMBERS AND BACK

