

Salamin-Brent Algorithm

initial values: $a_0 = 1$, $b_0 = \frac{1}{\sqrt{2}}$, $s_0 = \frac{1}{2}$

Repeat:

iteration
1

$$a_1 = \frac{a_0 + b_0}{2} = \frac{1 + \frac{1}{\sqrt{2}}}{2}$$

$$b_1 = \sqrt{a_0 b_0} = \sqrt{1 \cdot \frac{1}{\sqrt{2}}} = \sqrt{\frac{1}{\sqrt{2}}}$$

$$s_1 = \frac{1}{2} - 2' (a_1^2 - b_1^2) = \frac{1}{2} - 2 \left(\left(\frac{1 + \frac{1}{\sqrt{2}}}{2} \right)^2 - \left(\sqrt{\frac{1}{\sqrt{2}}} \right)^2 \right)$$

$$p_1 = \frac{2a_1^2}{s_1} = \frac{2 \left(\frac{1 + \frac{1}{\sqrt{2}}}{2} \right)^2}{s_1} = 3.187\dots$$

iteration
2

$$a_2 = \dots$$

$$b_2 = \dots$$

$$s_2 = \dots$$

$$p_2 = \dots$$