

5 April 2024

An integer  $n \geq 2$  is **prime** if its only divisors are 1 and itself.

An integer  $n \geq 2$  is **composite** if it has a divisor other than 1 and  $n$ .

Note: 1 is neither prime nor composite (by definition).

How to determine whether a number is prime?

example:  $n = 2,931,133 = 1031 \cdot 2843$

idea: check for divisors, but this might take a while

## CURRENT RECORDS

- Arbitrary numbers up to 200 digits or so can be factored.
- Feb. 2020: RSA-250 (250 digits, 2 prime factors) was factored.  
This took 2700 core-years of computing time.
- Arbitrary numbers of more than 15,000 digits can be proven prime.
- Largest known prime:  $2^{82589933} - 1$  (Dec. 2018)  
this has 24,862,048 digits

Write a function:  $\text{isPrime}(n)$

INPUT: integer  $n \geq 2$

OUTPUT: True if  $n$  is prime,

False otherwise

Return  
value