

2. The joint pdf of X and Y is $f(x, y) = 3x$, for $0 \leq y \leq x \leq 1$.

(a) What is the conditional distribution of X given $Y = y$?

(b) What are $E(X | Y = y)$? and $\text{Var}(X | Y = y)$?

3. For continuous random variables X and Y , show that $E(E(X | Y)) = E(X)$.

4. The number of eggs N found in nests of a certain species of turtles has a Poisson distribution with mean λ . Each egg has probability p of being viable, and this event is independent from egg to egg. Find the mean and the variance of the number of viable eggs per nest.

★ **BONUS:** If X and Y are independent binomial random variables with identical parameters n and p , calculate the conditional expected value of X given that $X + Y = m$.